

The GNSS - TEC analysis of the paroxysmal eruptive activity of Mt. Etna

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The ionosphere

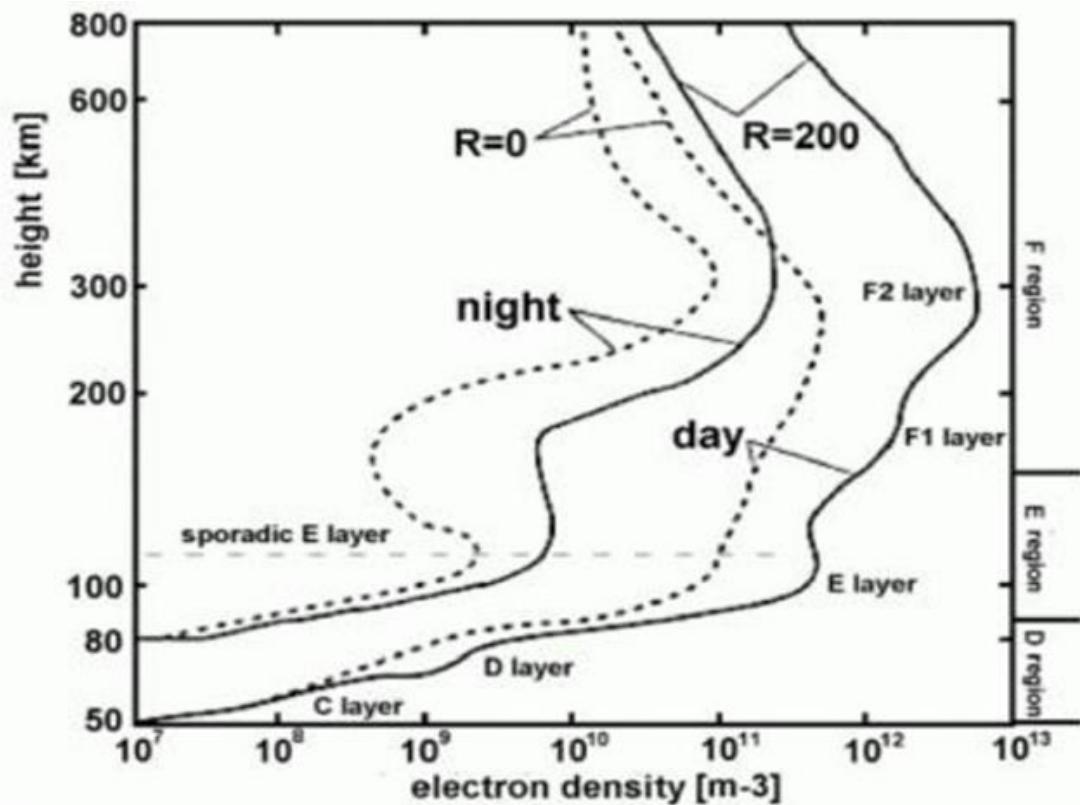
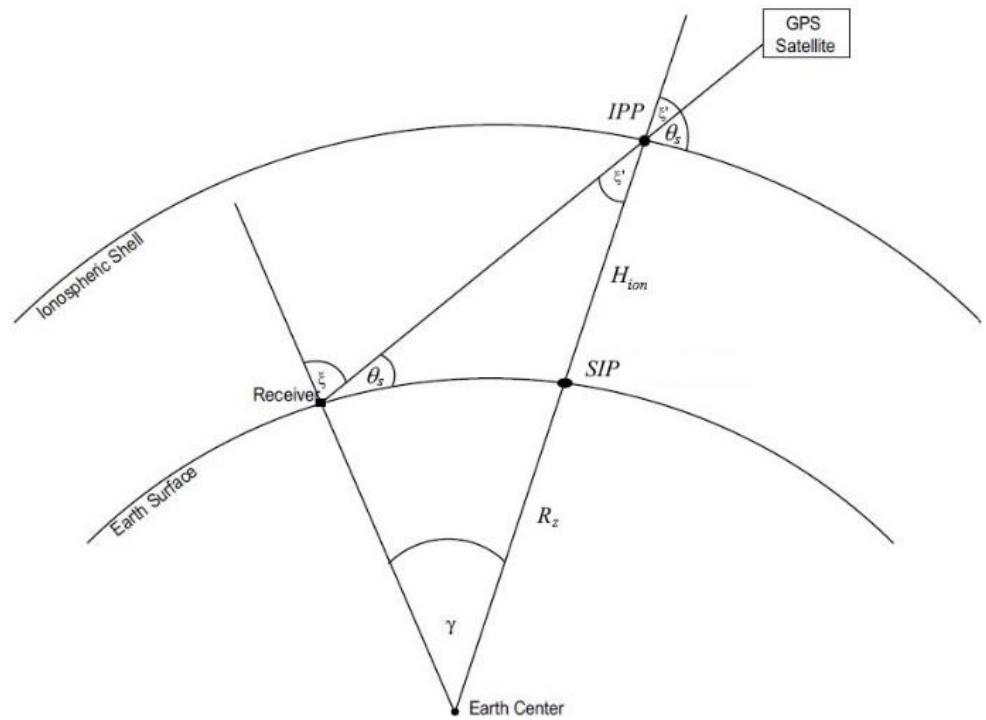


Figure from INGV

- 50 – 1000 km of altitude (mesosphere – thermosphere – esosphere)
- **Plasma** composed by free electrons and ions (UV, X solar and cosmic radiations)
- Electron density influenced by solar activity (R) and daytime
- **Dispersive medium** for the GNSS signal

The Total Electron Content (TEC)



- Integral of the number of electrons along the satellite – receiver line of sight for a **referee ionospheric height** H_{ion} (ionospheric shell)
- 1 TECu (TEC unit) = $1 \cdot 10^{16} e^-/m^2$
- $H_{ion} \sim 300$ km of altitude
- IPP (Ionospheric Pierce Point)
- SIP (Sub-ionospheric Pierce Point)
- θ (satellite elevation angle)

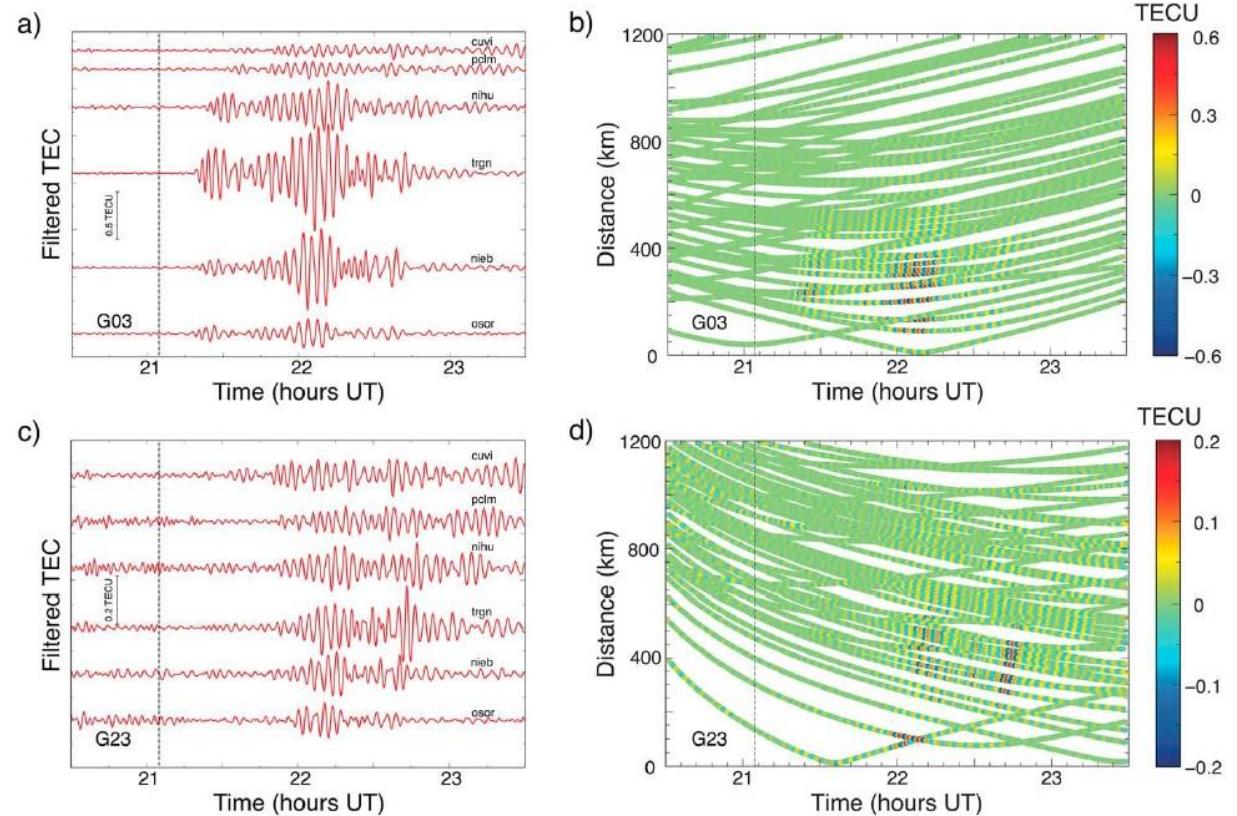
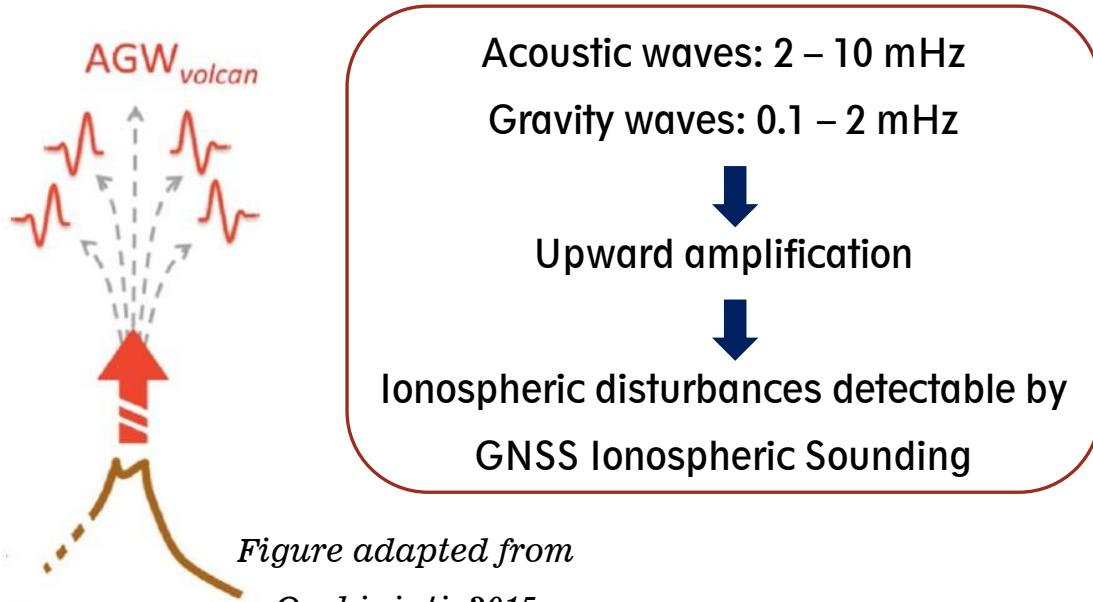
Figure adapted from Dautermann & Calais, 2008

Co-Volcanic Ionospheric Disturbances (CVIDs)

Ionospheric electron density oscillations caused by **Acoustic-Gravity Waves** (AGW) propagation from volcanic eruptions

TEC peaks proportional to **VEI (Volcanic Explosivity Index)**

- Velocity $\sim 550 - 1200$ m/s (AGW – AW – Shock AW)
- T period $\sim 12 - 30$ min.
- First arrival time to H_{ion} about 10 to 45 min



Shults et al., 2015

The VARION algorithm

Variometric Approach for Real-time Ionosphere ObservatioN

$$L_{4R}^S(t+1) - L_{4R}^S(t) = \frac{f_{L1}^2 - f_{L2}^2}{f_{L2}^2} [I_{1R}^S(t+1) - I_{1R}^S(t)]$$



$$\delta sTEC(t+1, t) = \frac{f_L^1 f_L^2 f_{L2}^2}{A(f_{L1}^2 - f_{L2}^2)} [L_{4R}^S(t+1) - L_{4R}^S(t)]$$



$$\Delta TEC(t_f, t_0) = \int_{t_0}^{t_f} \delta TEC(t)$$

Single time difference of **geometry-free combinations** of GNSS carrier-phase measurements

- f_1, f_2 (carrier frequencies)
- I (ionospheric delay)

TEC variation between two epochs

- A (ionospheric constant)

TEC variation over a chosen time range

Ravanelli et al., 2021

Etna – 4 December 2015 (I episode)



Photo © Giuseppe Mario Famiani

Large Scale Lava Fountain (LSLF) eruptive style

- very high, dense eruptive column
- abundant coarse-grained tephra fallout up to the lower slopes
- ash dispersal up to hundreds of kilometers

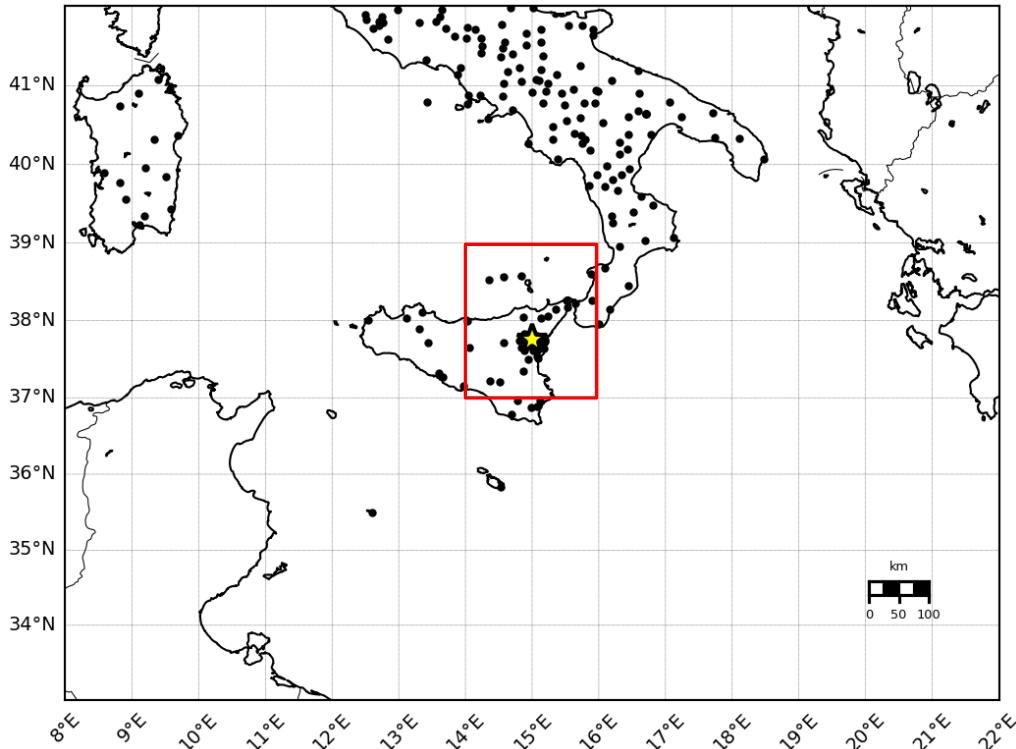
Andronico et al., 2021

Data from Calvari et al. (2018) and from courtesy of Scollo & Mereu***

Crater	Start seismo-acoustic activity (UTC)	End seismo-acoustic activity (UTC)	Mean wind velocity (m/s) **	Mean height fountain (m) *	Max height fountain (m) *	Plume height (km) **	Pyroclastic volume (m³) *	Max Q _m (kg/s) **	Max RMS_seismic (m/s)	Max RMS_infrasound (Pa)
Voragine	08:40	11:00	7.5	1264	2600	13.1	2760000	$1.62 \cdot 10^6$	$5.54 \cdot 10^{-5}$	13.78

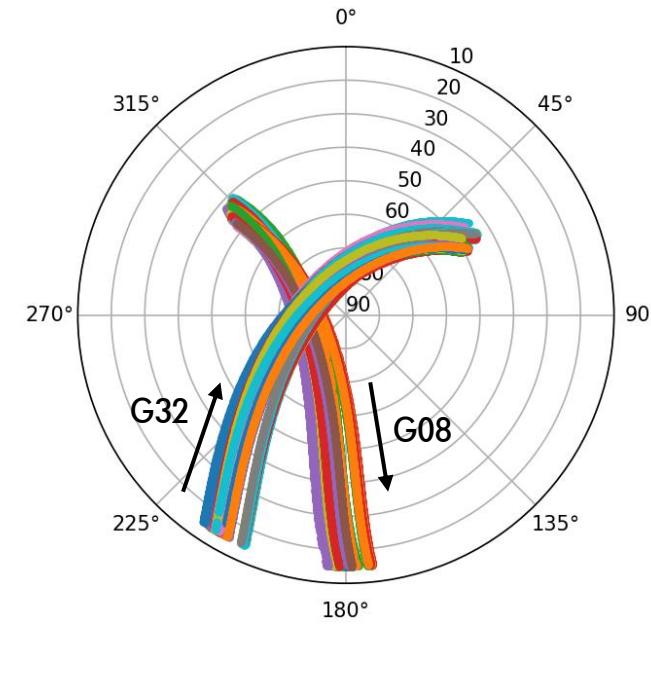
Dataset

RINEX (Receiver INdependent EXchange format) data at 30 s

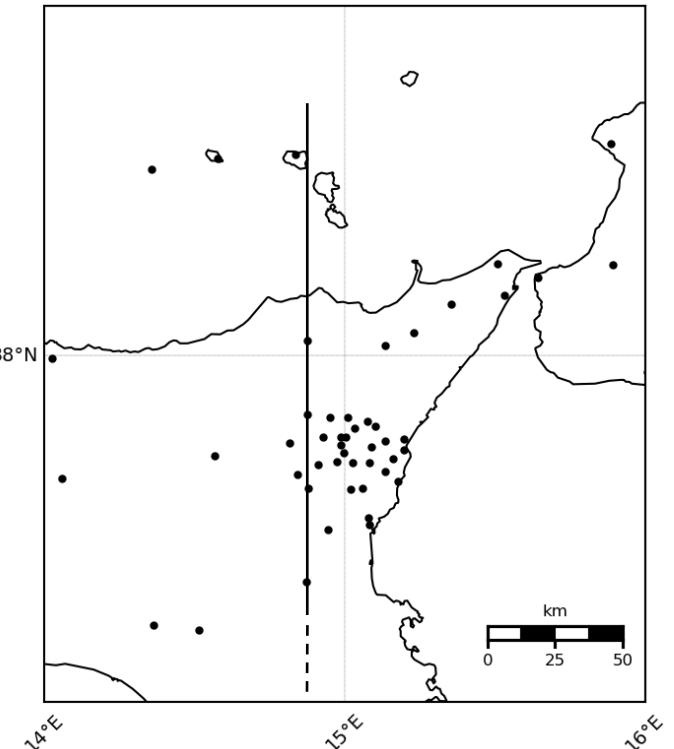


197 receivers

- 28 INGV-OE (GPS)
- 16 ASI (Euref net - GNSS)
- 54 Topcon (GNSS)
- 99 RING (GNSS)



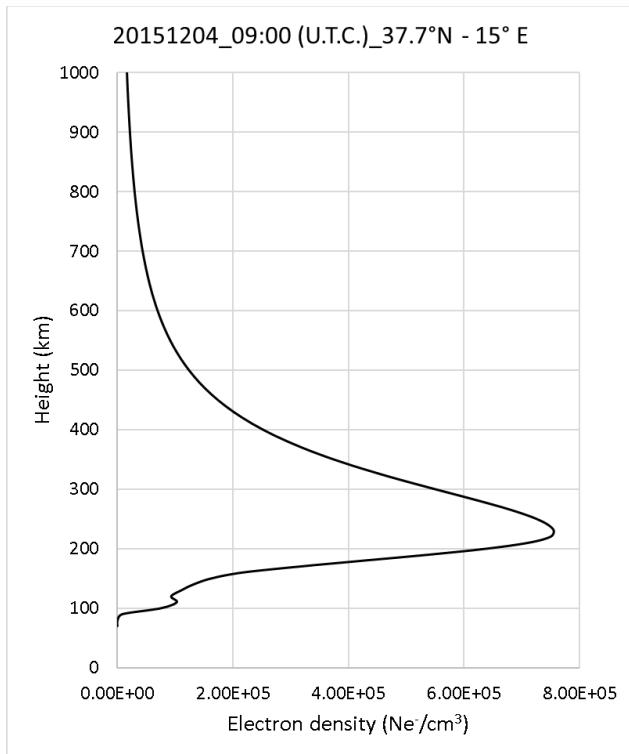
G08 – G32
Ionospheric Sounding



North - South profile

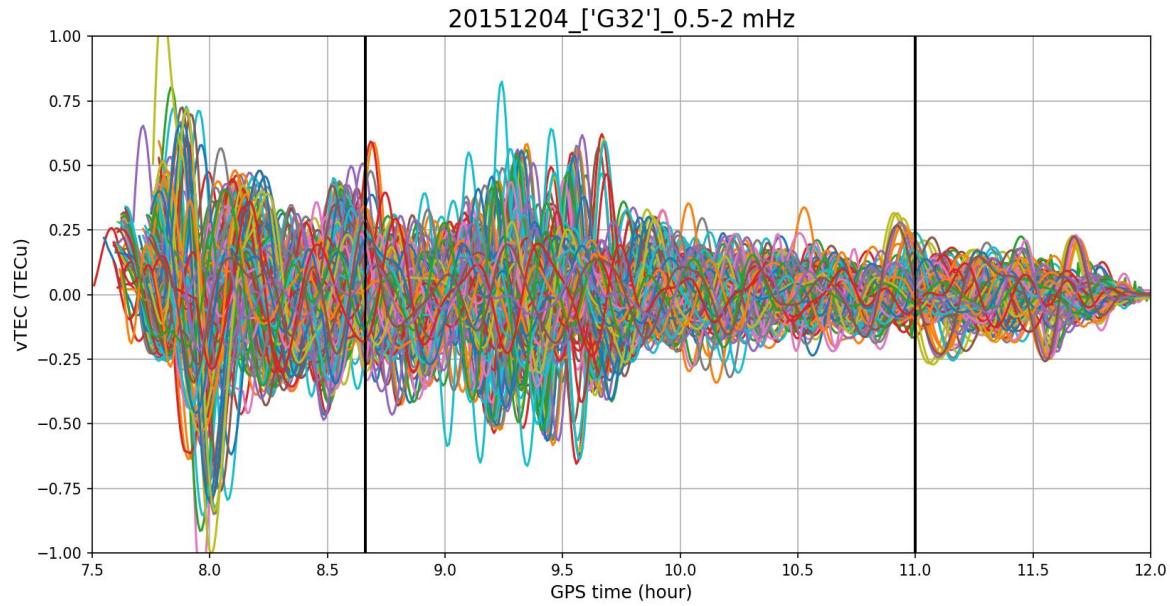
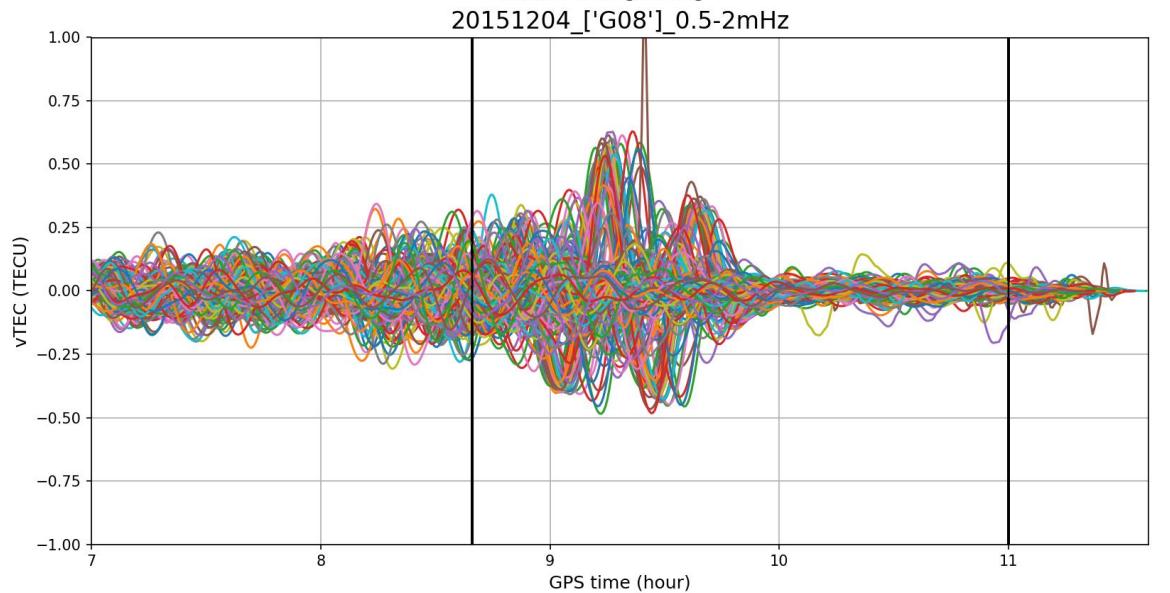
TEC time series

TEC peaks about **0.5 TECu** in 0.5 – 2 mHz frequency range



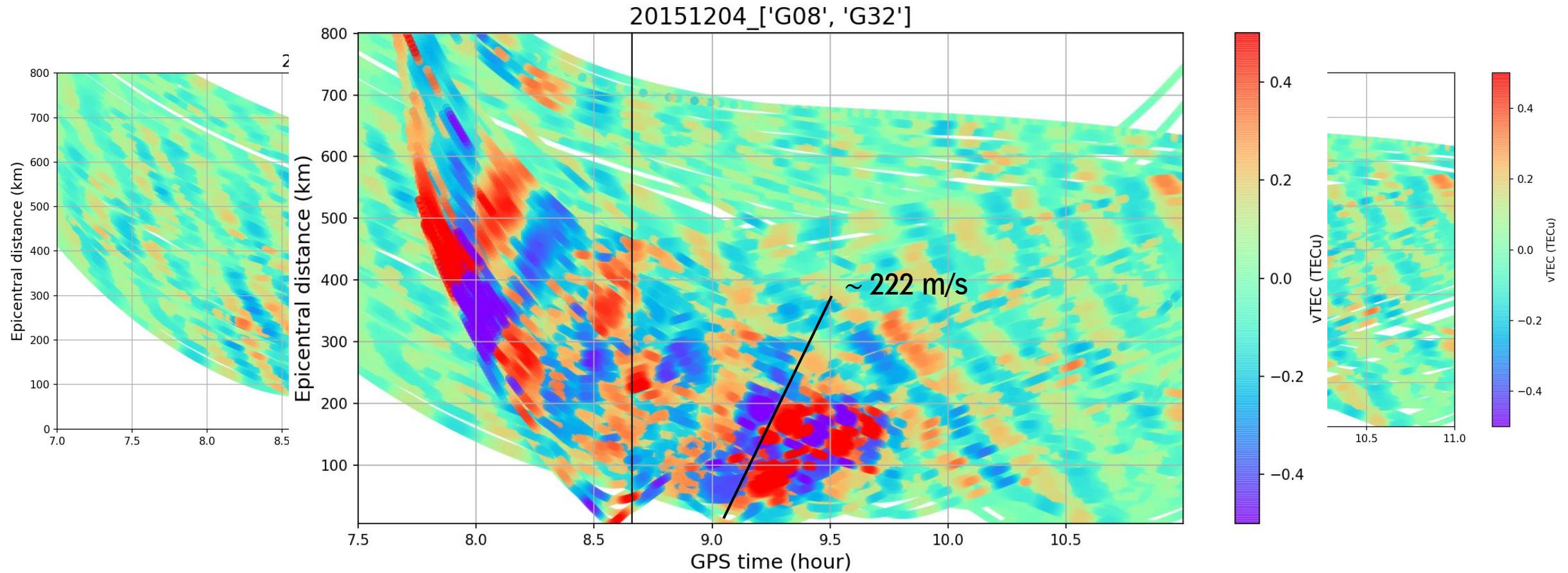
$$H_{\text{ion}} = 230 \text{ km s.l.m.}$$

Data from IRI 2016



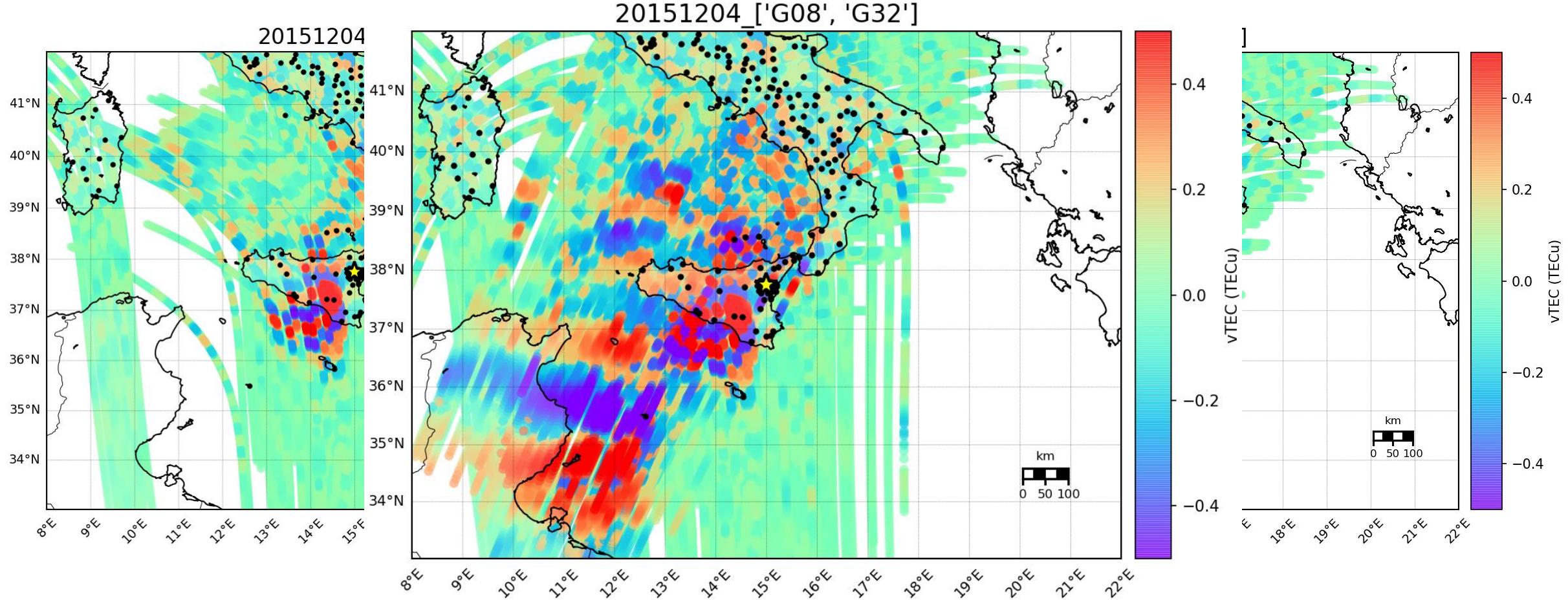
Hodochrones

Apparent horizontal velocity at about 222 m/s



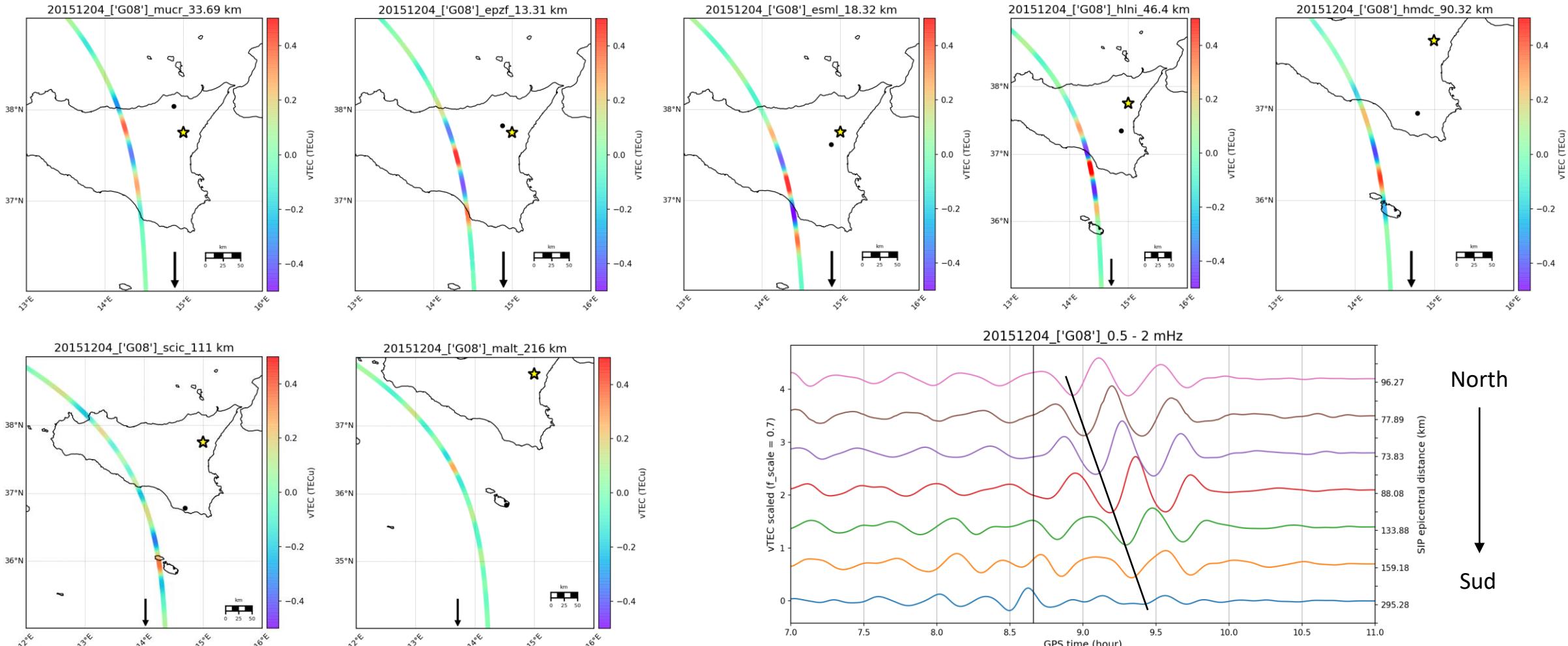
SIP maps

Local vTEC anomalies (0.5 – 2mHz) in the South near field, up to about 200 km from Etna



G08 - SIP trajectories and wave forms

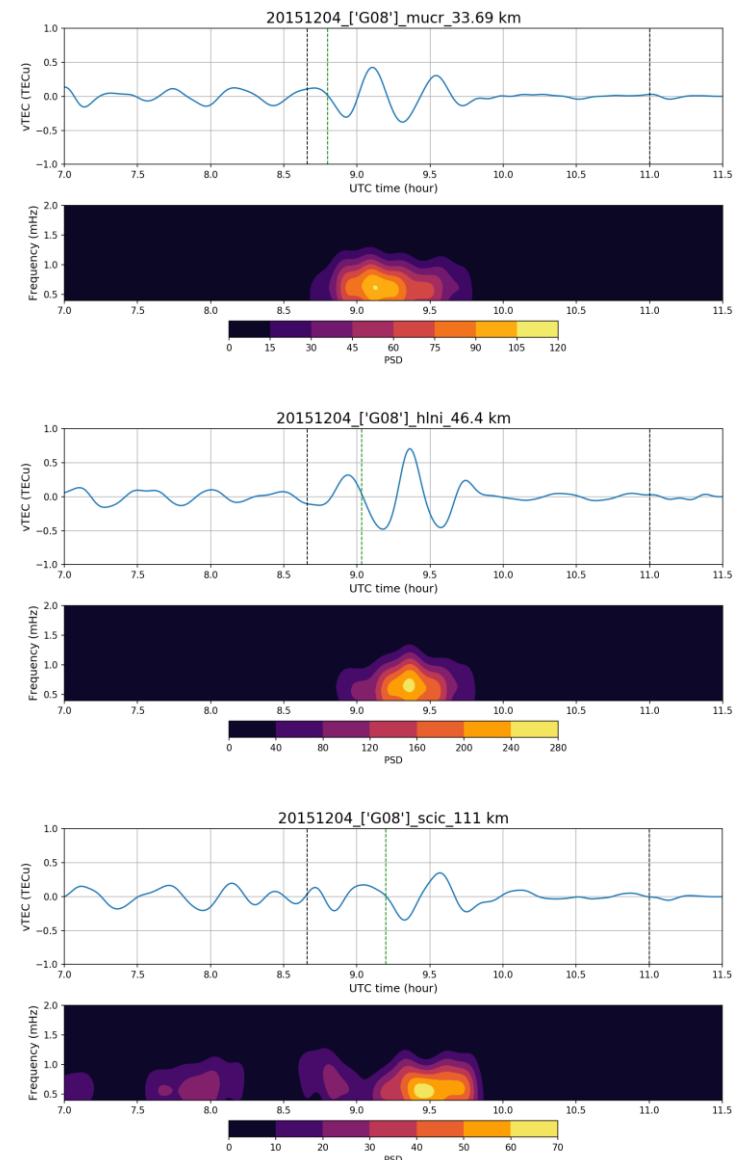
Wave propagation southward for about 30 minutes



G08 - spectrograms and frequency peaks

Stable frequency content at 0.6 mHz for vTEC peaks

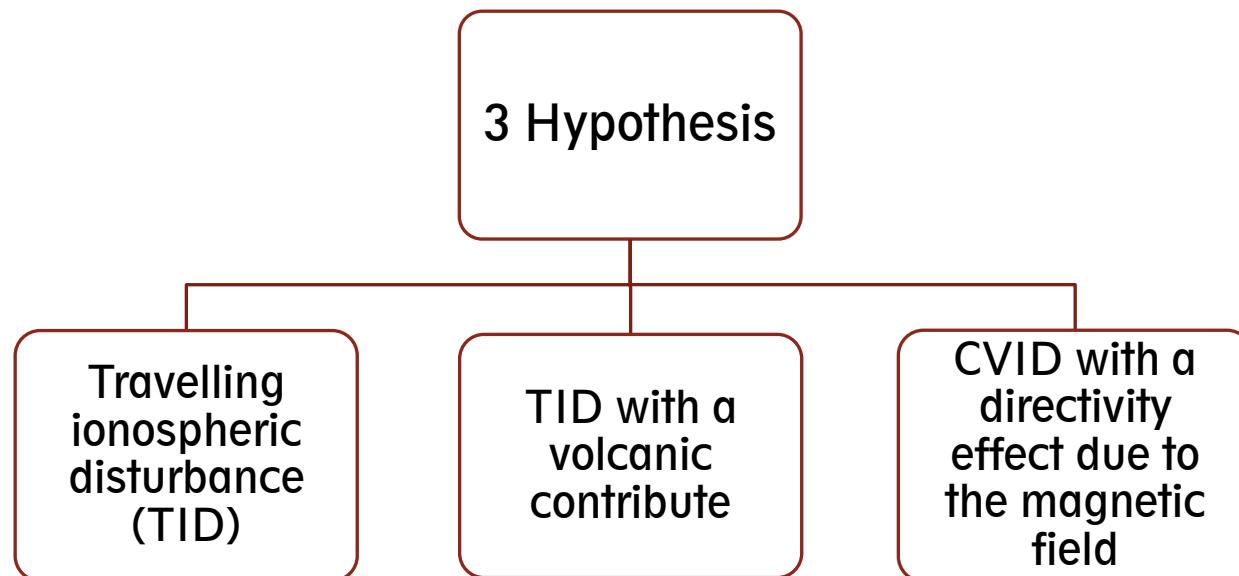
Station	Picking time (U.T.C.)	SIP epi_distance (km)	vTEC peak (TECu)	Peak frequency (mHz)	PSD peak
MUCR	08:47:55	96.27	0.43	0.61	156.46
EPZF	08:53:00	77.9	0.62	0.66	192.67
ESML	08:56:30	73.84	0.68	0.64	226.63
HLNI	09:02:04	88.09	0.7	0.66	250.04
HMDC	09:09:00	133.88	0.43	0.61	118.49
SCIC	09:12:00	159.19	0.35	0.55	66.28
MALT	09:28:56	294	0.12	0.67	7.38



Conclusions and outlook

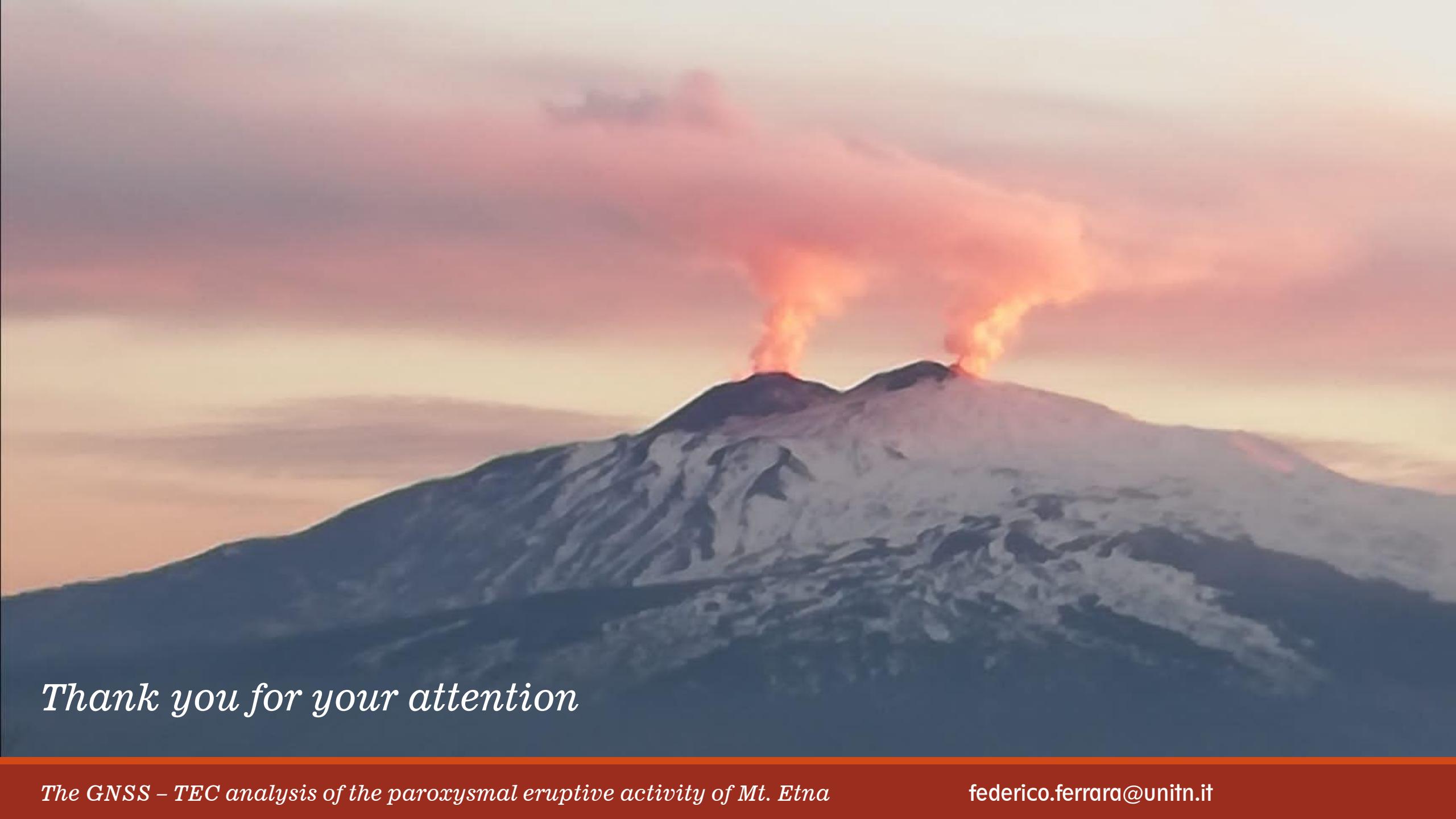
Conclusions:

- **Gravity waves propagation** with most frequency content at 0.6 mHz
- **Directivity** of the vTEC peak towards South-West principally



Outlook:

- Source characterization
- Constellation satellite geometric features
- Directivity effects by geomagnetic field
- Other Etna paroxysmal activities data
- Other ionospheric data
- **Time relation source – ionosphere**



Thank you for your attention