



DEVELOPMENTS IN
PETROLEUM SCIENCE

36

**THE PRACTICE OF
RESERVOIR
ENGINEERING
(REVISED EDITION)**

L.P. DAKE





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