



An Introduction to  
**THE MECHANICS OF SOILS  
AND FOUNDATIONS**  
Through Critical State Soil Mechanics

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